**Solutions Manual** 

to accompany Principles of Highway Engineering and Traffic Analysis, 4e

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# Chapter 2 Road Vehicle Performance

**U.S. Customary Units** 

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## Preface

The solutions to the fourth edition of *Principles of Highway Engineering and Traffic Analysis* were prepared with the Mathcad<sup>1</sup> software program. You will notice several notation conventions that you may not be familiar with if you are not a Mathcad user. Most of these notation conventions are self-explanatory or easily understood. The most common Mathcad specific notations in these solutions relate to the equals sign. You will notice the equals sign being used in three different contexts, and Mathcad uses three different notations to distinguish between each of these contexts. The differences between these equals sign notations are explained as follows.

- The ':=' (colon-equals) is an assignment operator, that is, the value of the variable or expression on the left side of ':='is set equal to the value of the expression on the right side. For example, in the statement, L := 1234, the variable 'L' is assigned (i.e., set equal to) the value of 1234. Another example is x := y + z. In this case, x is assigned the value of y + z.
- The '=' (bold equals) is used when the Mathcad function solver was used to find the value of a variable in the equation. For example, in the equation

 $5.2 \cdot t - 0.005 \cdot t^2 = 18.568 + 10 \cdot (t - 12.792)$ , the = is used to tell Mathcad that the value of the expression on the left side needs to equal the value of the expression on the right side. Thus, the Mathcad solver can be employed to find a value for the variable 't' that satisfies this relationship. This particular example is from a problem where the function for arrivals at some time 't' is set equal to the function for departures at some time 't' to find the time to queue clearance.

The '=' (standard equals) is used for a simple numeric evaluation. For example, referring to the x := y + z assignment used previously, if the value of y was 10 [either by assignment (with :=), or the result of an equation solution (through the use of =) and the value of z was 15, then the expression 'x =' would yield 25. Another example would be as follows: s := 1800/3600, with s = 0.5. That is, 's' was assigned the value of 1800 divided by 3600 (using :=), which equals 0.5 (as given by using =).

Another symbol you will see frequently is ' $\rightarrow$ '. In these solutions, it is used to perform an evaluation of an assignment expression in a single statement. For example, in the following statement,  $Q(t) := \text{Arrivals}(t) - \text{Departures}(t) \rightarrow 2.200 \cdot t - .1000 \cdot t^2$ , Q(t) is assigned the value of Arrivals(t) – Departures(t), and this evaluates to  $2.2t - 0.10t^2$ .

Finally, to assist in quickly identifying the final answer, or answers, for what is being asked in the problem statement, yellow highlighting has been used (which will print as light gray).

<sup>1</sup> www.mathcad.com

## Determine the power required to overcome aerodynamic drag.

$$p := 0.002378$$
  $C_D := 0.29$   $A_f := 20$  ft<sup>2</sup> (given)  
 $V := 100 \cdot \frac{5280}{3600}$  ft/s  $V = 146.7$   
solve for horsepower  
 $hp := \frac{p \cdot C_D \cdot A_f \cdot V^3}{1100}$  (Eq. 2.4)

hp = 39.6

1100

## Problem 2.2

(given)

#### Determine the final weight of the car.

$$\rho := 0.002378 \ C_D := 0.30 \ A_f := 21 \ W_o := 2100 \ V_{max} := 100 \cdot \frac{5280}{3600}$$

Add one horsepower per 2 lbs. additional vehicle weight

Solve for additional weight added to the vehicle, set resistance forces equal to additional hp

$$\frac{550 \text{ W}_{a}}{2} = \frac{\rho}{2} \cdot \text{C}_{D} \cdot \text{A}_{f} \cdot \left(\text{V}_{max}\right)^{3} + 0.01 \cdot \left(1 + \frac{\text{V}_{max}}{147}\right) \cdot \left(\text{W}_{o} + \text{W}_{a}\right) \cdot \text{V}_{max}$$

$$W_{a} = 109.48$$

$$\text{Total} := W_{o} + W_{a}$$

$$\text{Total} = 2209.48$$
Ib

# Determine the distance from the vehicle's center of gravity to the front axle.

FWD F<sub>max</sub> = RWD F<sub>max</sub>

$$\frac{\frac{\mu W(l_{f}-f_{fl}\cdot h)}{L}}{1-\frac{\mu \cdot h}{L}} = \frac{\frac{\mu W(l_{r}+f_{fl}\cdot h)}{L}}{1+\frac{\mu \cdot h}{L}}$$
(Eq. 2.14)

solve for Ir in terms of L and If left with one unknown (Ir)

 $I_{\mathbf{f}} \coloneqq L - I_{\mathbf{f}}$ 



#### Determine the minimum coefficient of road adhesion.

$$F = ma + R_{rl} = rear F_{max} = \frac{\mu W(l_r f_{rl} h)/L}{1 - \mu h/L}$$
(Eq. 2.14)

substitute for m, R<sub>rl</sub>

$$m := \frac{W}{g} \qquad R_{rl} := f_{rl} \cdot W \qquad (Eq. 2.6)$$

$$\frac{W}{g} \cdot a + f_{rl} \cdot W = \frac{\frac{\mu \cdot W \cdot (I_{f} - f_{rl} \cdot h)}{L}}{1 - \frac{\mu \cdot h}{L}}$$

μ = 0.637 <sub>∎</sub>

# Determine the distance from the vehicle's center of gravity to the rear axle.

$$F = ma + R_{rl} = rear F_{max} = \frac{\mu W(l_f f_{rl}h)/L}{1 - \mu h/L}$$
(Eq. 2.14)

substitute for m, R<sub>rl</sub>

$$m := \frac{W}{g} \qquad R_{fl} := f_{fl} \cdot W \qquad (Eq. 2.6)$$

$$\frac{W}{g} \cdot a + f_{fl} \cdot W = \frac{\frac{\mu \cdot W \cdot (I_{f} - f_{fl} \cdot h)}{L}}{1 - \frac{\mu \cdot h}{L}}$$

$$I_{f} = 166 \qquad \text{inches}$$

Determine the lowest gear reduction ratio.

$$\label{eq:W} \begin{split} W &:= 2700 \quad r := \frac{14}{12} \qquad L := 8.2\cdot 12 \eqno(given) \\ \mu &:= 1.0 \quad h := 18 \qquad f_{fl} := 0.01 \quad l_f := 3.3\cdot 12 \end{split}$$

$$F = \operatorname{rear} F_{\max} = \frac{\mu W(l_f f_{rl}h)/L}{1 - \mu h/L}$$
(Eq. 2.14)

"highest possible acceleration" means  $\rm F_e$  is equal to  $\rm F_{max}$ 

$$\mathsf{F}_{\max} \coloneqq \frac{\frac{\mu \cdot \mathsf{W} \cdot \left(\mathsf{I}_{\mathsf{f}} - \mathsf{f}_{\mathsf{f}} \cdot \mathsf{h}\right)}{\mathsf{L}}}{1 - \frac{\mu \cdot \mathsf{h}}{\mathsf{L}}}$$

F<sub>max</sub> = 1323.806

$$M_e := 540$$
  $\eta_d := 0.95$  (given)

solve for  $\varepsilon_0$ 

$$F_{max} = \frac{M_e \cdot \epsilon_0 \cdot \eta_d}{r} \qquad \qquad \epsilon_0 := \frac{F_{max} \cdot r}{M_e \cdot \eta_d} \qquad (Eq. 2.17)$$

ε<sub>ο</sub> = 3∎

Determine the maximum acceleration from rest.

$$\begin{aligned} \epsilon_0 &:= 9 & r := \frac{14}{12} & g := 32.2 & \mu := 1.0 & f_{rl} := 0.01 \\ h &:= \frac{18}{12} & l_f := 4.3 & L := 9.2 & W := 2450 \\ R_{rl} &:= W \cdot f_{rl} & R_{rl} = 24.5 & (Eq. 2.6) \end{aligned}$$

M<sub>ebase</sub> := 185 M<sub>emod</sub> := 215 η<sub>d</sub> := 0.90

solve for mass factor

$$\gamma_{\rm m} := 1.04 + 0.0025 \cdot \varepsilon_0^2 \qquad \gamma_{\rm m} = 1.24$$
 (Eq. 2.20)

$$F_{ebase} := \frac{M_{ebase} \cdot \epsilon_0 \cdot \eta_d}{r} \quad F_{ebase} = 1284.43$$
 (Eq. 2.17)

$$F_{max} := \frac{\frac{\mu \cdot W \cdot (I_{f} - f_{fl} \cdot h)}{L}}{1 - \frac{\mu \cdot h}{L}} \qquad F_{max} = 1363.41 \qquad (Eq. 2.14)$$

since  $F_{ebase} < F_{max}$ , use  $F_{ebase}$  for calculating acceleration with original engine

$$a_{base} := \frac{F_{ebase} - R_{rl}}{\gamma_{m} \cdot \left(\frac{W}{g}\right)} \qquad a_{base} = 13.33 \qquad \frac{ft}{s^{2}}$$
(Eq. 2.19)

$$F_{emod} := \frac{M_{emod} \cdot \epsilon_0 \cdot \eta_d}{r} \qquad F_{emod} = 1492.71 \qquad (Eq. 2.17)$$

since  $F_{emod} > F_{max}$ , use  $F_{max}$  for calculating acceleration with modified engine

$$a_{\text{mod}} := \frac{F_{\text{max}} - R_{\text{rl}}}{\gamma_{\text{m}} \cdot \left(\frac{W}{g}\right)} \qquad \begin{array}{c} a_{\text{mod}} = 14.16 & \frac{ft}{s^2} \\ & s^2 \end{array}$$
(Eq. 2.19)

#### Determine the maximum acceleration rate.

$$i := 0.035$$
  $n_e := 50$   $\epsilon_0 := 3.5$   $r := \frac{15}{12}$   $g := 32.2$  (given)

solve for velocity

$$V := \frac{2 \cdot \pi \cdot r \cdot n_{e} \cdot (1 - i)}{\epsilon_{0}} \qquad V = 108.3$$
 (Eq. 2.18)

$$\rho := 0.002378 \quad C_{D} := 0.35 \quad A_{f} := 21$$

calculate aerodynamic resistance

$$R_a := \frac{\rho}{2} \cdot C_D \cdot A_f \cdot V^2$$
  $R_a = 102.45$  (Eq. 2.3)

calculate rolling resistance

$$f_{rl} := 0.01 \left( 1 + \frac{V}{147} \right)$$
 W := 3000 (Eq. 2.5)  
 $R_{rl} := f_{rl} \cdot W$   $R_{rl} = 52.1$ 

calculate mass factor

$$\gamma_{\rm m} := 1.04 + 0.0025 \cdot \varepsilon_0^2 \qquad \gamma_{\rm m} = 1.07$$
 (Eq. 2.20)

calculate engine-generated tractive effort

$$F_e := \frac{M_e \cdot \varepsilon_0 \cdot n_d}{r} \qquad F_e = 630 \qquad (Eq. 2.17)$$

$$F_{net} = F - \sum_{n} R = \gamma_{m} \cdot m \cdot a$$
  
so  $a := \frac{F_{e} - R_{a} - R_{rl}}{\gamma_{m} \cdot \left(\frac{W}{g}\right)}$   $a = 4.77 \frac{ft}{sec^{2}}$  (Eq. 2.19)

## Determine the drag coefficient.

$M_e := 150  \epsilon_0 := 3.0  \eta_d := 0.90  r := \frac{15}{12}$	(given)
$i := 0.02$ W := 2150 $n_e := \frac{4500}{60}$	
$V := \frac{2 \cdot \pi \cdot r \cdot n_e \cdot (1 - i)}{\varepsilon_0} \qquad V = 192.4$	(Eq. 2.18)
$F_e := \frac{M_e \cdot \epsilon_0 \cdot \eta_d}{r}$ $F_e = 324$	(Eq. 2.17)
$f_{rl} := 0.01 \cdot \left( 1 + \frac{V}{147} \right)$	(Eq. 2.5)
$R_{rl} := f_{rl} \cdot W$ $R_{rl} = 49.643$	(Eq. 2.6)
ρ := 0.002378 A <sub>f</sub> := 19.4	

 $\mathsf{F}_{\mathsf{e}} = \mathsf{R}_{\mathsf{f}} + \frac{\rho}{2} \cdot \mathsf{C}_{\mathsf{D}} \cdot \mathsf{A}_{\mathsf{f}} \cdot \mathsf{V}^{2} \qquad \qquad \mathsf{C}_{\mathsf{D}} \coloneqq \frac{2(\mathsf{F}_{\mathsf{e}} - \mathsf{R}_{\mathsf{f}})}{\mathsf{A}_{\mathsf{f}} \cdot \mathsf{V}^{2} \cdot \rho}$ 

C<sub>D</sub> = 0.321

## Determine the drag coefficient.

## Problem 2.10

$$M_e := 200 \quad \epsilon_o := 3.0 \quad n_d := 0.90 \quad r := \frac{14}{12}$$
 (given)

$$F_e := \frac{M_e \cdot \varepsilon_0 \cdot n_d}{r}$$
  $F_e = 462.9$  (Eq. 2.17)

V := 150 · 1.467 W := 2500 
$$f_{rl} := 0.01 \cdot \left(1 + \frac{V}{147}\right)$$
 (Eq. 2.5)

$$R_{rl} := f_{rl} \cdot W$$
  $R_{rl} = 62.423$  (Eq. 2.6)

set  $\rm F_e$  equal to the sum of the resistance forces and solve for  $\rm C_D$ 

$$\mathsf{F}_{e} = \mathsf{R}_{\mathsf{rl}} + \frac{\rho}{2} \cdot \mathsf{C}_{\mathsf{D}} \cdot \mathsf{A}_{\mathsf{f}} \cdot \mathsf{V}^{2} \qquad \qquad \mathsf{C}_{\mathsf{D}} \coloneqq \frac{2(\mathsf{F}_{e} - \mathsf{R}_{\mathsf{rl}})}{\mathsf{A}_{\mathsf{f}} \cdot \mathsf{V}^{2} \cdot \rho}$$

C<sub>D</sub> = 0.278

#### Determine the maximum grade.

### Problem 2.11

i := 0.035  $n_e := \frac{3500}{60} \epsilon_o := 3.2$   $r := \frac{14}{12}$  W:= 2500 lb (given)

assume F=F<sub>e</sub>

calculate velocity

$$\bigvee_{i=1}^{\infty} = \frac{2 \cdot \pi \cdot r \cdot n_{e} \cdot (1-i)}{\varepsilon_{o}} \qquad V = 128.9 \qquad \text{ft/s} \tag{Eq. 2.18}$$

calculate aerodynamic resistance

$$\label{eq:relation} \begin{split} \rho &:= 0.002378 \quad C_D := 0.35 \quad A_f := 25 \\ R_a &:= \frac{\rho}{2} \cdot C_D \cdot A_f \cdot V^2 \qquad R_a = 172.99 \quad \text{Ib} \end{split} \tag{Eq. 2.3}$$

calculate rolling resistance

$$f_{rl} := 0.01 \left( 1 + \frac{V}{147} \right)$$
 (Eq. 2.5)  
 $R_{rl} := f_{rl} \cdot W$   $R_{rl} = 46.93$  lb

calculate engine-generated tractive effort

$$M_e := 200$$
  $n_d := 0.90$   
 $F_e := \frac{M_e \cdot \varepsilon_0 \cdot n_d}{r}$   $F_e = 493.71$  lb (Eq. 2.17)

calculate grade resistance

$$R_{g} \coloneqq F_{e} - R_{a} - R_{rl}$$
(Eq. 2.2)  

$$R_{g} = 273.79$$
solve for G  

$$R_{a}$$

$$\mathbf{G} \coloneqq \frac{\mathbf{W}}{\mathbf{W}}$$
(Eq. 2.9)

G = 0.1095 therefore G = 11.0%

#### Alternative calculation for grade, using trig relationships

$$\boldsymbol{\theta}_{g} := asin \left( \frac{R_{g}}{W} \right)$$

 $\theta_g = 0.1097$  radians

 $deg\theta_g := \theta_g \cdot \frac{180}{\pi} \qquad \text{ convert from radians to degrees}$ 

 $\text{deg}\theta_g=6.287$ 

tan deg = opposite side/adjacent side

 $\mathbf{G} := \tan(\theta_{\mathbf{g}}) \cdot 100$   $\mathbf{G} = 11.02$  %

Thus, error is minimal when assuming G = sin  $\, \theta_g$  for small to medium grades

#### Determine the torque the engine is producing and the engine speed.

$$F_e - \Sigma R = \gamma_m \cdot m \cdot a$$

at top speed, acceleration = 0; thus,  $F_e - \Sigma R = 0$ 

$$V_{\text{min}} := 124 \cdot \frac{5280}{3600} \quad V = 181.867 \quad \text{ft/s}$$
 (given)

calculate aerodynamic resistance

$$\rho := 0.00206 \quad C_D := 0.28 \quad A_f := 19.4$$

$$R_a := \frac{\rho}{2} \cdot C_D \cdot A_f \cdot V^2 \qquad R_a = 185.056 \quad (Eq. 2.3)$$

calculate rolling resistance

$$f_{rl} := 0.01 \cdot \left( 1 + \frac{V}{147} \right) \qquad f_{rl} = 0.022 \qquad (Eq. 2.5)$$

$$W := 2700 \qquad (given)$$

$$R_{rl} := f_{rl} \cdot W \qquad R_{rl} = 60.404 \qquad (Eq. 2.6)$$

$$R_{g} := 0$$

sum of resistances is equal to engine-generated tractive effort, solve for Me

$$F_{e} := R_{a} + R_{rl} + R_{g} \qquad F_{e} = 245.46 \qquad (Eq. 2.2)$$
  
$$i := 0.03 \qquad \eta_{d} := 0.90 \qquad \underset{\text{RQA}}{\&} := 2.5 \qquad r := \frac{12.6}{12}$$

$$F_{e} = \frac{M_{e} \cdot \varepsilon_{0} \cdot \eta_{d}}{r} \qquad \qquad M_{e} := \frac{F_{e} \cdot r}{\varepsilon_{0} \cdot \eta_{d}} \qquad (Eq. 2.17)$$

$$M_{e} = 114.548 \qquad \text{ft-lb}$$

Knowing velocity, solve for ne

$$V = \frac{2 \cdot \pi \cdot r \cdot n_{e} \cdot (1 - i)}{\varepsilon_{0}} \qquad n_{e} := \frac{V \cdot \varepsilon_{0}}{2 \cdot \pi \cdot r \cdot (1 - i)} \qquad (Eq. 2.18)$$

$$n_{e} = 71.048 \qquad \frac{rev}{s} \qquad n_{e} \cdot 60 = 4263 \qquad \frac{rev}{min}$$

#### Determine the maximum acceleration from rest.

$$F_{max} := \frac{\frac{\mu \cdot W \cdot (I_{f} - f_{fl} \cdot h)}{L}}{1 - \frac{\mu \cdot h}{L}} \qquad F_{max} = 859.62 \qquad (Eq. 2.14)$$

For maximum torque, derivative of torque equation equals zero

$$\frac{dM_e}{dn_e} = 6 - 0.09n_e = 0 \qquad n_e := \frac{6}{0.09} \qquad n_e = 66.67$$

plug this value into torque equation to get value of maximum torque

$$M_e := 6 \cdot n_e - 0.045 \cdot n_e^2$$
  $M_e = 200$ 

$$e_0 := 11$$
  $n_d := 0.75$   $r := \frac{14}{12}$ 

find engine-generated tractive effort from maximum torque

$$F_e := \frac{M_e \cdot \epsilon_0 \cdot n_d}{r}$$
  $F_e = 1414.29$  (Eq. 2.17)

$$F_e := \frac{W_e \cdot e_0 \cdot W_d}{r}$$
  $F_e = 1414.29$  (Eq. 2.17)

calculate rolling resistance and mass factor

$$R_{rl} := f_{rl} \cdot W$$
  $R_{rl} = 25$  (Eq. 2.6)

$$\gamma_{\rm m} := 1.04 + 0.0025 \cdot \varepsilon_0^2 \quad \gamma_{\rm m} = 1.34$$
 (Eq. 2.20)

calculate acceleration from maximum available tractive effort

$$a := \frac{F_{max} - f_{rl} \cdot W}{\gamma_{m} \cdot \left(\frac{W}{g}\right)} \qquad a = 8.01 \frac{ft}{\sec^2}$$
(Eq. 2.19)

## Determine speed of car.

Power = 
$$(2\pi M_e \cdot n_e) = 6.28 \cdot (6n_e^2 - 0.045n_e^3) = 37.68n_e^2 - 0.2826n_e^3$$
 (Eq. 2.16)  
P $(n_e) := 37.68n_e^2 - 0.2826n_e^3$ 

To find maximum power take derivative of power equation

$$\frac{d}{dn_e} P(n_e) \rightarrow 75.36 \cdot n_e - .8478 \cdot n_e^2 = 0$$

$$n_e := \frac{75.36}{0.8478}$$
  $n_e = 88.89$   
i := 0.035  $\epsilon_0 := 2$   $r := \frac{14}{12}$ 

Calculate maximum velocity at maximum engine power

$$V := \frac{2 \cdot \pi \cdot r \cdot n_{e} \cdot (1 - i)}{\epsilon_{0}}$$

$$V = 314.39 \quad \frac{ft}{s} \qquad \frac{V}{1.467} = 214.3 \quad \frac{mi}{h}$$
(Eq. 2.18)

(given)

#### Determine the acceleration for front- and rear-wheel-drive options.

$$M_e := 95 \quad \epsilon_0 := 4.5 \quad n_d := 0.80 \quad r := \frac{13}{12}$$
 (given)

 $\rm R_{a},\, \rm R_{rl},\, and\, g_{m}$  are as before

calculate engine-generated tractive effort

$$F_e := \frac{M_e \cdot e_0 \cdot n_d}{r}$$
  $F_e = 315.692$  (Eq. 2.17)

calculate maximum acceleration

$$a_{max} := \frac{F_e - R_a - R_{rl}}{\gamma_m \cdot \left(\frac{W}{g}\right)} \qquad a_{max} = 2.768 \tag{Eq. 2.19}$$

Rear - wheel drive

$$\mu := 0.2 \qquad f_{fl} := 0.011 \qquad h := 20 \qquad L := 120 \qquad l_f := 60$$

$$F_{max} := \frac{\frac{\mu \cdot W \cdot (I_{f} - f_{fl} \cdot h)}{L}}{1 - \frac{\mu \cdot h}{L}} \qquad F_{max} = 309.207$$

$$a_{max} := \frac{F_{max} - R_{a} - R_{fl}}{\gamma_{m} \cdot \left(\frac{W}{g}\right)} \qquad a_{max} = 2.704 \quad \frac{ft}{\sec^{2}} \qquad 2.704 < 2.768 \qquad (Eq. 2.19)$$

Front - wheel drive

.

$$F_{max} := \frac{\frac{\mu \cdot W \cdot (l_{f} + f_{fl} \cdot h)}{L}}{1 + \frac{\mu \cdot h}{L}} \qquad F_{max} = 291.387 \qquad (Eq. 2.15)$$

$$a_{max} := \frac{F_{max} - R_a - R_{fl}}{\gamma_{m} \cdot \left(\frac{W}{g}\right)} \qquad (Eq. 2.19)$$

$$a_{max} = 2.529 \qquad \frac{ft}{\sec^2} \qquad 2.529 < 2.768$$

### Determine weight and torque.

## Problem 2.16

$$\begin{split} \mu &:= 0.8 \quad W_0 := 2000 \quad \epsilon_0 := 10 \quad n_d := 0.8 \\ l_f &:= 55 \quad r := \frac{14}{12} \quad f_{fl} := 0.01 \quad h := 22 \quad L := 100 \end{split} \tag{given}$$

$$F_e = \frac{M_e \cdot \epsilon_0 \cdot n_d}{r} \tag{Eq. 2.17}$$

$$F_{max} = \frac{\frac{\mu \cdot W_a \cdot (l_f - f_{fl} \cdot h)}{L}}{1 - \frac{\mu \cdot h}{L}} \tag{Eq. 2.14}$$

 $I_{\text{fnew}} = I_{\text{f}} - \frac{3 \cdot 1}{20} \cdot M_{\text{e}} \qquad W_{\text{a}} = W_{\text{o}} + 3 \cdot M_{\text{e}}$ 

setting  $F_e = F_{max}$  and solving for  $M_e$  gives

$$\frac{M_{e} \cdot \varepsilon_{0} \cdot n_{d}}{r} = \frac{\frac{\mu \cdot (W_{0} + 3 \cdot M_{e}) \cdot \left[ \left( I_{f} - \frac{3 \cdot 1}{20} \cdot M_{e} \right) - f_{rl} \cdot h \right]}{L}}{1 - \frac{\mu \cdot h}{L}}$$

$$M_{e} = 122.152 \qquad \text{ft-lb}$$

$$W_a := W_0 + 3 \cdot M_e$$
  $W_a = 2366.5$  lb

Determine the difference in minimum theoretical stopping distances with and without aerodynamic resistance considered.

$$\begin{split} \rho &:= 0.0024 \qquad C_D := 0.45 \quad A_f := 25 \qquad V := 90 \cdot 1.467 \\ g &:= 32.2 \quad \gamma_b := 1.04 \qquad W := 2500 \qquad \eta_b := 1.0 \qquad (given) \\ f_{fl} &:= 0.019 \quad \mu := 0.7 \quad \theta := 5.71 \\ K_a &:= \frac{\rho}{2} \cdot C_D \cdot A_f \qquad K_a = 0.014 \qquad (Eq. 2.37) \end{split}$$

$$S := \frac{\gamma_b \cdot W}{2 \cdot g \cdot K_a} \cdot \ln \left( 1 + \frac{K_a \cdot V^2}{\eta_b \cdot \mu \cdot W + f_{rl} \cdot W - W \cdot sin(\theta \cdot deg)} \right) \qquad S = 423.027$$
(Eq. 2.42)

compared to S = 444.07 and S = 457.53

444.07 – 424.64 = 19.43 ft

457.53 - 424.64 = 32.89 ft

Determine the initial speed with and without aerodynamic resistance.

$$K_a := \frac{\rho}{2} \cdot C_D \cdot A_f$$
  $K_a = 0.013$  (Eq. 2.37)

with aerodynamic resistance considered

$$S = \frac{\gamma_b \cdot W}{2 \cdot g \cdot K_a} \cdot \ln \left( 1 + \frac{K_a \cdot V^2}{\mu \cdot \eta_b \cdot W + f_{rl} \cdot W} \right)$$
(Eq. 2.43)  
$$V = 80.362 \qquad \frac{V}{1.467} = 54.78$$

with aerodynamic resistance ignored

$$S = \frac{\gamma_b \cdot V^2}{2 \cdot g \cdot (\eta_b \cdot \mu + f_{fl})} \qquad V := \sqrt{\frac{S \cdot 2 \cdot g \cdot (\eta_b \cdot \mu + f_{fl})}{\gamma_b}} \qquad (Eq. 2.42)$$
$$V = 79.182 \qquad \frac{V}{1.467} = 53.98 \qquad \frac{mi}{h}$$

#### Determine the unloaded braking efficiency, ignoring aerodynamic resistance.

$$\mu := 0.75 \quad f_{rl} := 0.018 \quad \gamma_b := 1.04$$
 (given)  
 $\alpha := 32.2 \quad S := 200 \quad V := 60.1.467$ 

solve Eq. 2.43 for braking efficiency

$$S = \frac{\gamma_{b} \cdot V^{2}}{2 \cdot g \cdot (\eta_{b} \cdot \mu + f_{fl})} \qquad \qquad \eta_{b} \coloneqq \frac{\gamma_{b} \cdot V^{2}}{S \cdot 2 \cdot g \cdot \mu} - f_{fl} \qquad (Eq. 2.43)$$

 $\eta_{\rm h} = 0.8101$ 

η<sub>b</sub>·100 = 81.01 %

# Determine the braking efficiency. $\mu := 0.60 \qquad \gamma_b := 1.04 \qquad g := 32.2 \qquad S := 590 \qquad G := 0.03$ (given) $V_1 := 110 \cdot \frac{5280}{3600}$ $V_1 = 161.333$ $V_2 := 55 \cdot \frac{5280}{3600}$ $V_2 = 80.667$ $f_{rl} := 0.01 \cdot \left( \begin{array}{c} \frac{V_1 + V_2}{2} \\ 1 + \frac{147}{147} \end{array} \right) \qquad f_{rl} = 0.018$ (Eq. 2.5) solve for braking efficiency using theoretical stopping distance equation $S = \frac{\gamma_{b} \cdot \left(V_{1}^{2} - V_{2}^{2}\right)}{2 \cdot g \cdot (\eta_{b} \cdot \mu + f_{rl} - G)} \qquad \qquad \eta_{b} := \frac{\gamma_{b} \cdot \left(V_{1}^{2} - V_{2}^{2}\right)}{2 \cdot S \cdot g \cdot \mu} - f_{rl} + G$ (Eq. 2.43) η<sub>b</sub> = 0.9102 η<sub>b</sub>·100 = 91.02 %

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## Problem 2.20

#### Determine the maximum amount of cargo that can be carried.

$$\begin{split} & \bigvee_{1} \coloneqq 75 \cdot 1.467 \qquad & \bigvee_{1} = 110.025 \quad \text{ft/s} \qquad & \bigvee_{2} \coloneqq 0 \quad (\text{vehicle is assumed to stop}) \\ & \mu \coloneqq 0.95 \qquad & G \coloneqq -0.04 \qquad g \coloneqq 32.2 \qquad & (\text{given}) \\ & \gamma_{b} \coloneqq 1.04 \qquad & \eta_{b} \coloneqq 0.80 \qquad & S \coloneqq 300 \\ & \bigvee_{avg} \coloneqq \frac{\bigvee_{1} + \bigvee_{2}}{2} \qquad & \bigvee_{avg} = 55.013 \\ & f_{\text{fl}} \coloneqq 0.01 \cdot \left(1 + \frac{\bigvee_{avg}}{147}\right) \qquad & f_{\text{fl}} \equiv 0.0137 \qquad & (\text{Eq. } 2.5) \end{split}$$

solve for additional vehicle weight using theoretical stopping distance equation, ignoring aerodynamic resistance

$$S = \frac{\gamma_{b} \cdot V_{1}^{2}}{2 \cdot g \cdot \left[ \left( \eta_{b} - \frac{W}{100 \cdot 100} \right) \cdot \mu + f_{rl} + G \right]}$$
(Eq. 2.43)

W = 864.2 lb

Determine the speed of the car when it strikes the object.

$$\begin{split} & C_D \coloneqq 0.5 \quad A_f \coloneqq 25 \quad W \coloneqq 3500 \quad \rho \coloneqq 0.002378 \\ & S \coloneqq 150 \quad \mu \coloneqq 0.85 \quad g \coloneqq 32.2 \quad \gamma_b \coloneqq 1.04 \\ & f_{rl} \coloneqq 0.018 \quad \eta_b \coloneqq 0.80 \\ & V_1 \coloneqq 80 \cdot 1.467 \quad V_1 = 117.36 \end{split}$$
 (given)

$$K_a := \frac{\rho}{2} \cdot C_D \cdot A_f$$
  $K_a = 0.015$  (Eq. 2.37)

How fast will the car be travelling when it strikes the object on a level surface?

$$S = \frac{\gamma_b \cdot W}{2 \cdot g \cdot K_a} \cdot \ln \left[ \frac{\eta_b \cdot \mu \cdot W + K_a \cdot {V_1}^2 + f_{fl} \cdot W}{\eta_b \cdot \mu \cdot W + K_a \cdot ({V_2}^2) + f_{fl} \cdot W} \right]$$
(Eq. 2.39)  
$$V_2 = 82.967 \qquad \frac{V_2}{1.467} = 56.56 \qquad \frac{mi}{h}$$

How fast will the car be travelling when it strikes the object on a 5% grade?

$$G := 0.05$$

$$S = \frac{\gamma_b \cdot W}{2 \cdot g \cdot K_a} \cdot \ln \left[ \frac{\eta_b \cdot \mu \cdot W + K_a \cdot {V_1}^2 + f_{fl} \cdot W + G \cdot W}{\eta_b \cdot \mu \cdot W + K_a \cdot (V_2^2) + f_{fl} \cdot W + G \cdot W} \right]$$

$$V_2 = 80.176 \qquad \frac{V_2}{1.467} = 54.65 \qquad \frac{mi}{h}$$
(Eq. 2.39)

(given)

#### Determine the speed of the car just before it impacted the object.

Find velocity of the car when it starts to skid

\_ \_ \_ \_

$$S_{al} = \frac{\gamma_b \cdot \left(V_1^2 - V_2^2\right)}{2 \cdot g \cdot \left(\eta_b \cdot \mu_m + f_{rl} - 0.03\right)}$$
(Eq. 2.43)  

$$V_2 := \sqrt{V_1^2 - \frac{2 \cdot S_{al} \cdot g \cdot \left(\eta_b \cdot \mu_m + f_{rl} - 0.03\right)}{\gamma_b}}$$
  

$$V_2 = 74.82 \qquad V_2 \cdot \frac{3600}{5280} = 51.014 \qquad \frac{mi}{h}$$
  
Vehicle's velocity at start of skid is  $V_1 := 74.82$   
Find velocity when the vehicle strikes the object

$$S_{skid} = \frac{\gamma_{b} \cdot (V_{1}^{2} - V_{2}^{2})}{2 \cdot g \cdot (\eta_{b} \cdot \mu_{s} + f_{rl} - 0.03)}$$
(Eq. 2.43)  
$$V_{2} := \sqrt{V_{1}^{2} - \frac{2 \cdot S_{skid} \cdot g \cdot (\eta_{b} \cdot \mu_{s} + f_{rl} - 0.03)}{\gamma_{b}}}$$
  
$$V_{2} = 63.396$$
  
$$\frac{V_{2} \cdot \frac{3600}{5280} = 43.22}{\frac{mi}{h}}$$

h

#### Determine if the driver should appeal the ticket.

h

 $\mu$  := 0.6 (for good, wet pavement, and slide value because of skidding)

$$\gamma_{b} := 1.04$$
  $g := 32.2$ 

5280

$$V_2 := 40 \cdot \frac{5280}{3600}$$
  $V_2 = 58.667$  (given)  
 $\eta_b := 0.95$   $S_{tri} := 200$   $f_{ri} := 0.015$ 

Solve for the initial velocity of the car using theoretical stopping distance

$$S = \frac{\gamma_{b} \cdot \left(V_{1}^{2} - V_{2}^{2}\right)}{2 \cdot g \cdot \left(\eta_{b} \cdot \mu + f_{rl} - 0.04\right)} \qquad V_{1} := \sqrt{\frac{2 \cdot S \cdot g \cdot \left(\eta_{b} \cdot \mu + f_{rl} - 0.04\right)}{\gamma_{b}} + V_{2}^{2}} \qquad (Eq. 2.43)$$

$$V_{1} = 100.952$$

$$V_{1} = 100.952$$

No, the driver should not appeal the ticket as the initial velocity was higher than the speed limit, in addition to the road being wet.

# Determine the shortest distance from the stalled car that the driver could apply the brakes and stop before hitting it.

$$\begin{split} \eta_b &\coloneqq 0.90 \quad \gamma_b &\coloneqq 1.04 \quad f_{\text{rl}} &\coloneqq 0.013 \end{tabular} \tag{given} \\ V &\coloneqq 70 \cdot \frac{5280}{3600} \qquad V &= 102.667 \quad \text{ft/s} \\ S &\coloneqq 150 \quad g &\coloneqq 32.2 \\ \mu_{\text{dry}} &\coloneqq 1.0 \qquad \mu_{\text{wet}} &\coloneqq 0.9 \end{tabular} \tag{Table 2.4} \end{split}$$

$$S = \frac{\gamma_{b} \cdot \left(V_{1}^{2} - 0\right)}{2 \cdot g \cdot \left(\eta_{b} \cdot \mu_{wet} + f_{rl} - 0.03\right)} \qquad V_{1} := \sqrt{\frac{2 \cdot S \cdot g \cdot \left(\eta_{b} \cdot \mu_{wet} + f_{rl} - 0.03\right)}{\gamma_{b}}} \qquad (Eq. 2.43)$$

$$V_1 = 85.824$$
  $V_1 \cdot \frac{3600}{5280} = 58.516$  ft/s

Using this as final velocity, solve for distance to slow to this velocity

$$S = \frac{\gamma_{b} \cdot (V^{2} - V_{1}^{2})}{2 \cdot g \cdot (\eta_{b} \cdot \mu_{dry} + f_{rl} - 0.03)}$$
(Eq. 2.43)  

$$S = 58.062$$

Add this distance to the 150 ft of wet pavement,

150 + S = 208.06 ft

## Determine the braking efficiency of car 1.

$$\begin{split} \gamma_b &\coloneqq 1.04 \quad g \coloneqq 32.2 \quad V \coloneqq 60 \cdot 1.467 \quad V = 88.02 \quad \text{ft/s} \end{tabular} \\ t_{r1} &\coloneqq 2.5 \quad t_{r2} \coloneqq 2.0 \quad \eta_{b2} \coloneqq 0.75 \quad \mu \coloneqq 0.80 \\ f_{rl} &\coloneqq 0.01 \left(1 + \frac{V}{2 \cdot 147}\right) \quad f_{rl} = 0.013 \end{split} \tag{Eq. 2.5}$$

Total stopping distance is perception/reaction distance plus braking distance

Set stopping distance of two cars equal to each other and solve for  $\eta_{\rm b1}$ 

$$V \cdot t_{r1} + \frac{\gamma_b \cdot V^2}{2 \cdot g} \cdot \left(\frac{1}{\eta_{b1} \cdot \mu + f_{rl}}\right) = V \cdot t_{r2} + \frac{\gamma_b \cdot V^2}{2 \cdot g} \cdot \left(\frac{1}{\eta_{b2} \cdot \mu + f_{rl}}\right)$$
$$\eta_{b1} := \operatorname{Find}(\eta_{b1}) \qquad \frac{\eta_{b1} \cdot 100 = 96.06}{\eta_{b1} \cdot 100 = 96.06} \quad \%$$

Determine the studen	t's associated perception reaction time.	Problem 2.27
V <sub>1</sub> := 55·1.467	V <sub>1</sub> = 80.685 ft/s	
V <sub>2</sub> := 35·1.467	V <sub>2</sub> = 51.345 ft/s	(given)
g := 32.2 G := 0	a := 11.2 ft/s <sup>2</sup>	
Solve for distance to slo	ow from 55 mi/h to 35 mi/h	
$d := \frac{\left(V_{1}\right)^{2} - \left(V_{2}\right)^{2}}{2 \cdot a}$	-	(Eq. 2.45)

Subtract this distance from total distance to sign (600 ft) to find perception/reaction time

$$\begin{array}{ll} d_{\rm S}:=600 & ({\rm given}) \\ \\ d_{\rm r}:=d_{\rm S}-d & d_{\rm r}:=600-d & d_{\rm r}=427.06 \\ \\ t_{\rm r}:=\frac{d_{\rm r}}{V_1} & \underline{t_{\rm r}=5.29} & {\rm sec} & ({\rm Eq.}\ 2.49) \end{array}$$

#### Comment on the student's claim.

Method 1:

Find practical stopping distance

$$d := \frac{V_1^2}{2 \cdot a}$$
  $d = 470.77$  (Eq. 2.46)

Subtract this distance from the total sight distance and solve for perception/reaction time

$$\begin{array}{ll} d_{\rm S} := 590 \\ d_{\rm r} := d_{\rm S} - d & d_{\rm r} = 119.23 \\ t_{\rm r} := \displaystyle \frac{d_{\rm r}}{V_1} & t_{\rm r} = 1.16 \quad {\rm sec} \end{array} \tag{Eq. 2.49}$$

This reaction time is well below the design value; therefore, the student's claim is unlikely.

Method 2:

V<sub>1</sub> := 70·1.467

g := 32.2 a := 11.2 G := 0 t<sub>r</sub> := 2.5

Stopping sight distance = practical stopping distance plus perception/reaction distance

$$SSD := \frac{V_1^2}{2 \cdot g \cdot \left[\left(\frac{a}{g}\right) + G\right]} + V_1 \cdot t_r \qquad SSD = 727.49 \quad \text{ft}$$
(Eq. 2.47)

590 ft < 730 ft (required from Table 3.1) therefore 590 ft is not enough for 70 mi/h design speed.

## Problem 2.28

#### Determine the grade of the road.

## Problem 2.29

$$V_1 := 55 \cdot 1.467$$
  $V_1 = 80.69$  ft/s (given)  
 $t_r := 2.5$   $d_s := 450$ 

Solve for distance travelled during braking (total distance minus perception/reaction)

$$d_r := V_1 \cdot t_r$$
  $d_r = 201.71$  (Eq. 2.49)  
 $d := d_s - d_r$   $d = 248.29$  (Eq. 2.50)

Using practical stopping distance formula and solve for grade

$$d = \frac{(V_1)^2}{2 \cdot g \cdot \left(\frac{a}{g} + G\right)} \qquad G := \frac{V_1^2}{2 \cdot d \cdot g} - \frac{a}{g} \qquad (Eq. 2.47)$$

$$G = 0.059 \qquad G \cdot 100 = 5.93 \qquad \%$$

<u>Determine the driver's perception/reaction time before and after drinking.</u>			Problem 2.30	
V <sub>1</sub> := 55·1.467	ft/s	g := 32.2	a := 11.2	(given)

while sober,  $d_s := 520$ 

solve for perception/reaction time using total stopping distance formula

$$d := \frac{V_1^2}{2 \cdot a}$$
 (Eq. 2.46)

$$d_s \coloneqq d_r + d$$
  $d_r \coloneqq d_s - d$  (Eq. 2.50)

$$d_r := \bigvee_1 \cdot t_r \qquad \qquad t_r := \frac{d_r}{\bigvee_1}$$
(Eq. 2.49)

substituting Eqs. 2.46 and 2.50 into Eq. 2.49 gives

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$$t_r := \frac{d_s}{V_1} - \frac{V_1}{2a}$$
  $t_r = 2.84$  sec (Eq. 2.50)

after drinking, driver strikes the object at  $V_2 := 35 \cdot 1.467$  ft/s

solve for perception/reaction time using total stopping distance formula

$$t_r := \frac{d_s}{V_1} - \frac{{V_1}^2 - {V_2}^2}{2a \cdot V_1}$$
  $t_r = 4.3$  sec (Eq. 2.50)

## **Multiple Choice Problems**

Determine the minimum t	Problem 2.31	
$C_{D} := 0.35$ $A_{f} := 20$ ft <sup>2</sup>	$\rho := 0.002045  \frac{\text{slugs}}{\text{ft}^3}$	(given)
$\mathbf{W} = 70 \cdot \left(\frac{5280}{3600}\right) \qquad \qquad \frac{\text{ft}}{\text{s}}$		
<u> </u>		
grade resistance		
$R_g := 2000  G$	$R_g = 100 lb$	(Eq. 2.9)
aerodynamic resistance		
$\mathbf{R}_{a} := \frac{\rho}{2} \cdot \mathbf{C}_{D} \cdot \mathbf{A}_{f} \cdot \mathbf{V}^{2}$	R <sub>a</sub> = 75.44 lb	(Eq. 2.3)
rolling resistance		
$f_{rl} := 0.01 \cdot \left(1 + \frac{V}{147}\right)$	$f_{rl} = 0.02$	(Eq. 2.5)
$\mathbf{R}_{rl} := \mathbf{f}_{rl} \cdot \mathbf{W}$	$R_{rl} = 33.97$ lb	(Eq. 2.6)
summation of resistances		
$\mathbf{K} := \mathbf{R}_a + \mathbf{R}_{rl} + \mathbf{R}_g$	F = 209.41 lb	(Eq. 2.2)

Alternative Answers:

1) Using mi/h instead of ft/s for velocity

$$\underbrace{V}_{\text{with}} = 70 \quad \frac{\text{mi}}{\text{h}}$$

$$\underbrace{f}_{\text{with}} = 0.01 \cdot \left(1 + \frac{\text{V}}{147}\right) \qquad f_{\text{rl}} = 0.01$$

- $R_{rl} = f_{rl} \cdot W$   $R_{rl} = 29.52$  lb
- $\mathbf{R}_{a} \coloneqq \frac{\rho}{2} \cdot \mathbf{C}_{D} \cdot \mathbf{A}_{f} \cdot \mathbf{V}^{2} \qquad \mathbf{R}_{a} = 35.07 \quad \text{lb}$

$$\mathbf{F} \coloneqq \mathbf{R}_a + \mathbf{R}_{rl} + \mathbf{R}_g \qquad \mathbf{F} = 164.6 \quad \text{lb}$$

2) not including aerodynamic resistance

$$W = 70 \frac{5280}{3600}$$
  
 $F = R_{rl} + R_g$   $F = 129.52$  lb

3) not including rolling resistance

$$F := R_a + R_g \qquad F = 135.07 \text{ lb}$$

#### Determine the acceleration.

## Problem 2.32

$$\begin{split} & \bigvee_{s} = 20 \cdot \frac{5280}{3600} & C_{d} := 0.3 & h := 20 \text{ in} \\ & V = 29.33 \quad \frac{ft}{s} & A_{f} := 20 \quad ft^{2} & \bigvee_{s} := 2500 \text{ lb} \\ & A_{f} := 20 \quad ft^{2} & \bigcup_{s} := 110 \text{ in} \\ & \rho := 0.002045 \quad \frac{slugs}{ft^{3}} & l_{f} := 50 \text{ in} \\ & M_{e} := 95 \quad ft \text{-lb} & \varepsilon_{o} := 4.5 \\ & r := \frac{14}{12} & ft & \eta_{d} := 0.90 \end{split}$$

#### aerodynamic resistnace

$$R_a := \frac{\rho}{2} \cdot C_d \cdot A_f \cdot V^2$$
  $R_a = 5.28$  lb (Eq. 2.3)

#### rolling resistance

$$f_{rl} := 0.01 \left( 1 + \frac{V}{147} \right)$$
(Eq. 2.5)  
$$R_{rl} := 0.01 \left( 1 + \frac{V}{147} \right) \cdot 2500 \qquad R_{rl} = 29.99 \quad lb \qquad (Eq. 2.6)$$

#### engine-generated tractive effort

$$F_e := \frac{M_e \cdot \varepsilon_o \cdot \eta_d}{r} \qquad \qquad F_e = 329.79 \quad lb \qquad \qquad (Eq. 2.17)$$

#### mass factor

$$\gamma_{\rm m} := 1.04 + 0.0025 {\epsilon_0}^2 \qquad \gamma_{\rm m} = 1.09$$
 (Eq. 2.20)  
 $l_{\rm r} := 120 - l_{\rm f}$ 

#### acceleration

$$F_{\max} := \frac{\frac{\mu \cdot W \cdot (l_r + f_{rl} \cdot h)}{L}}{1 + \frac{\mu \cdot h}{L}} \qquad F_{\max} = 1350.77 \quad lb \qquad (Eq. 2.15)$$
$$a := \frac{F_e - R_a - R_{rl}}{\gamma_m \cdot (\frac{2500}{32.2})} \qquad a = 3.48 \quad \frac{ft}{s^2} \qquad (Eq. 2.19)$$

Alternative Answers:

1) Use a mass factor of 1.04 
$$\gamma_{max} = 1.04$$
  $a = \frac{F_e - R_a - R_{rl}}{\gamma_m (\frac{2500}{32.2})}$   $a = 3.65 \frac{ft}{s^2}$ 

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2) Use 
$$F_{\text{max}}$$
 instead of  $F_{\text{e}}$   
 $\chi_{\text{max}} = 1.091$   $a = \frac{F_{\text{max}} - R_{\text{a}} - R_{\text{rl}}}{\gamma_{\text{m}} \cdot \left(\frac{2500}{32.2}\right)}$   $a = 15.53$   $\frac{\text{ft}}{\text{s}^2}$ 

3) Rear wheel instead of front wheel drive

$$F_{\text{max}} \coloneqq \frac{\frac{\mu \cdot W \cdot \left(l_{f} - f_{rl} \cdot h\right)}{L}}{1 - \frac{\mu \cdot h}{L}} \qquad F_{\text{max}} = 1382.22 \qquad a \coloneqq \frac{F_{\text{max}} - R_{a} - R_{rl}}{\gamma_{m} \cdot \left(\frac{2500}{32.2}\right)} \qquad a = 15.9 \qquad \frac{ft}{s^{2}}$$

Determine the percentage of braking force.		Problem 2.33
$\mathcal{M} := 65 \cdot \frac{5280}{3600}  \frac{\text{ft}}{\text{s}}$	$\mu := 0.90$	
L:= 120 in	$l_f := 50$ in	(given)
h := 20 in	$l_r := L - l_f$ in	
determine the coefficient of rolling	g resistance	
$\mathbf{f}_{\mathbf{rl}} \coloneqq 0.01 \cdot \left(1 + \frac{\mathbf{V}}{147}\right)$	$f_{rl} = 0.02$	(Eq. 2.5)
determine the brake force ratio		
$BFR_{frmax} \coloneqq \frac{l_r + h \cdot (\mu + f_{rl})}{l_f - h \cdot (\mu + f_{rl})}$	BFR <sub>frmax</sub> = 2.79	(Eq. 2.30)
calculate percentage of braking f	orce allocated to rear axle	
$PBF_r := \frac{100}{1 + BFR_{frmax}}$	PBF <sub>r</sub> = 26.39 %	(Eq. 2.32)
Alternative Answers:		
1) Use front axle equation		
$PBF_{f} \coloneqq 100 - \frac{100}{1 + BFR_{frmax}}$	$PBF_{f} = 73.61 $ %	(Eq 2.31)
2) Use incorrect brake force ratio	equation	
$\underset{l_{f}}{\text{BFR}_{\text{finances}}} \coloneqq \frac{l_{r} - h \cdot \left(\mu + f_{rl}\right)}{l_{f} + h \cdot \left(\mu + f_{rl}\right)}$	$BFR_{frmax} = 0.76$	
$\frac{\text{PBF}}{\text{MMMM}} = \frac{100}{1 + \text{BFR}_{\text{frmax}}}$	PBF <sub>r</sub> = 56.94 %	
3) Switch I <sub>f</sub> and I <sub>r</sub> in brake force r	atio equation	
$\texttt{BFR}_{\texttt{frames}} \coloneqq \frac{l_f + h \cdot \left(\mu + f_r \right)}{l_r - h \cdot \left(\mu + f_r \right)}$	BFR <sub>frmax</sub> = 1.32	
$PBF_{\text{MM}} := \frac{100}{1 + BFR_{\text{frmax}}}$	$PBF_{r} = 43.06$ %	

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Determine the theoretical stopping distance on level grade.		Problem 2.34
$C_{D} := 0.59$ $A_{f} := 26 \text{ ft}^{2}$	$ \underbrace{W}_{s} = 80 \cdot \frac{5280}{3600}  \frac{\text{ft}}{\text{s}} $ $ \mu := 0.7 $	(given)
γ <sub>b</sub> := 1.04	$\eta_b := 0.75$	(assumed values)
Coefficient of Rolling Re	esistance	
$f_{rl} := 0.01 \cdot \left( \frac{\frac{V}{2}}{1 + \frac{2}{147}} \right)$	$f_{rl} = 0.014$	(Eq. 2.5)
D		
Theoretical Stopping Di	istance	
$\mathbf{x} \coloneqq \frac{\gamma_{b} \cdot \left( V_{1}^{2} - V_{2}^{2} \right)}{2 \cdot g \cdot \left( \eta_{b} \cdot \mu + f_{rl} \right)}$	$S = 412.8 \frac{s^2}{ft}$	(Eq. 2.43)
Alternative Answers:		
1) Not dividing the veloci	ty by 2 for the coeffeicent of rolling resistance	
$(\mathbf{v})$		

$$f_{\text{MM}} := 0.01 \cdot \left(1 + \frac{V}{147}\right)$$

$$s_{\text{M}} := \frac{\gamma_{\text{b}} \cdot \left(V_1^2 - V_2^2\right)}{2 \cdot g \cdot \left(\eta_{\text{b}} \cdot \mu + f_{\text{rl}}\right)} \qquad S = 409.8 \frac{s^2}{\text{ft}}$$

2) Using mi/h instead of ft/s for the velocity

$$\begin{aligned} &\underbrace{\mathbf{W}}_{\mathbf{k}} \coloneqq 80 \qquad \underbrace{\mathbf{W}}_{\mathbf{k}} \coloneqq 80 \\ &\underbrace{\mathbf{f}}_{\mathbf{k}} \coloneqq 0.01 \cdot \left(1 + \frac{\underline{\mathbf{V}}}{147}\right) \\ &\underbrace{\mathbf{S}}_{\mathbf{k}} \coloneqq \frac{\gamma_{\mathbf{b}} \cdot \left(\underline{\mathbf{V}}_{1}^{2} - \underline{\mathbf{V}}_{2}^{2}\right)}{2 \cdot \mathbf{g} \cdot \left(\eta_{\mathbf{b}} \cdot \mu + \mathbf{f}_{\mathbf{r}}\right)} \end{aligned} \qquad \mathbf{S} = 192.4 \frac{\mathbf{s}^{2}}{\mathbf{ft}} \end{aligned}$$

3) Using  $\gamma = 1.0$  value

$$\chi_{\text{Max}} := 1.0$$

$$\chi_{\text{S}} := \frac{\gamma_{\text{b}} \cdot \left(V_1^2 - V_2^2\right)}{2 \cdot g \cdot \left(\eta_{\text{b}} \cdot \mu + f_{\text{rl}}\right)}$$

$$S = 397.9 \frac{s^2}{\text{ft}}$$

## Determine the stopping sight distance.

## Problem 2.35

$$W = 45 \frac{5280}{3600} \quad \text{ft/s} \qquad (given)$$

$$a := 11.2 \quad \frac{ft}{s^2} \qquad t_r := 2.5 \quad \text{s} \qquad g_r := 32.2 \quad \frac{ft}{s^2} \qquad (assumed)$$
Braking Distance
$$d := \frac{v^2}{2 \cdot g \cdot \left(\frac{a}{g}\right)} \qquad d = 194.46 \quad \text{ft} \qquad (Eq. 2.47)$$
Perception/Reaction Distance
$$d_r := V \cdot t_r \qquad d_r = 165.00 \quad \text{ft} \qquad (Eq. 2.49)$$
Total Stopping Distance
$$d_s := d + d_r \qquad d_s = 359.46 \quad \text{ft} \qquad (Eq. 2.50)$$
Alternative Answers:
1) just the braking distance value
$$d = 194.46 \quad \text{ft}$$
2) just the perception/reaction distance value
$$d_r = 165.00 \quad \text{ft}$$

3) use the yellow signal interval deceleration rate

$$a_{m} := 10.0$$

$$d_{m} := \frac{V^{2}}{2 \cdot g \cdot \left(\frac{a}{g}\right)}$$

$$d_{s} := d + d_{r}$$

$$d_{s} = 382.80 \quad \text{ft}$$

## Determine the vehicle speed.

## Problem 2.36

$$\begin{split} & C_{D} \coloneqq 0.35 & G_{c} \coloneqq 0.04 & \gamma_{b} \coloneqq 1.04 \\ & A_{f} \coloneqq 16 \quad ft^{2} & S_{c} \coloneqq 150 \quad ft & \eta_{b} \coloneqq 1 & (given) \\ & W_{c} \coloneqq 2500 \quad lb & \rho \coloneqq 0.002378 \quad \frac{slugs}{ft^{3}} & \mu \coloneqq 0.8 \\ & V_{1} \coloneqq 88 \cdot \frac{5280}{3600} \quad \frac{ft}{s} & g_{c} \coloneqq 32.2 \quad \frac{ft}{s^{2}} & f_{1} \coloneqq 0.017 \end{split}$$

$$\mathbf{K}_{\mathbf{a}} \coloneqq \frac{\rho}{2} \cdot \mathbf{C}_{\mathbf{D}} \cdot \mathbf{A}_{\mathbf{f}} \qquad \mathbf{K}_{\mathbf{a}} = 0.007$$

$$V_{2} := 0$$

$$S = \frac{\gamma_{b} \cdot W}{2 \cdot g \cdot K_{a}} \cdot \ln \left[ \frac{\eta_{b} \cdot \mu \cdot W + K_{a} \cdot V_{1}^{2} + f_{rl} \cdot W + W \cdot G}{\eta_{b} \cdot \mu \cdot W + K_{a} \cdot \left(V_{2}^{2}\right) + f_{rl} \cdot W + W \cdot G} \right]$$

$$W_{2} := \operatorname{Find}(V_{2})$$

$$V_{2} = 91.6$$

$$\frac{V_{2}}{1.467} = 62.43$$

$$\frac{\operatorname{mi}}{h}$$
(Eq. 2.39)

#### Alternative Answers:

#### 1) Use 0% grade

G := 0.0

Given

$$V_2 = 0$$

$$S = \frac{\gamma_b \cdot W}{2 \cdot g \cdot K_a} \cdot \ln \left[ \frac{\eta_b \cdot \mu \cdot W + K_a \cdot V_1^2 + f_{rl} \cdot W + W \cdot G}{\eta_b \cdot \mu \cdot W + K_a \cdot (V_2^2) + f_{rl} \cdot W + W \cdot G} \right]$$

$$V_{2x} = Find(V_2)$$
  
 $V_2 = 93.6$   $\frac{V_2}{1.467} = 63.78$ 

2) Ignoring aerodynamic resistance

mi h

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3) Ignoring aerodynamic resistance and using G = 0

$$\mathcal{N}_{2a} := \sqrt{V_1^2 - \frac{S \cdot 2 \cdot g \cdot (\eta_b \cdot \mu + f_{r1} + G)}{\gamma_b}} \qquad V_2 = 95.2$$
$$\frac{V_2}{1.467} = 64.9 \qquad \frac{mi}{h}$$