

# Chapter 1

1. Compute the indicated value of the given function.

$$f(x) = 2x^2 - x; f(-1)$$

Ans: 3

Difficulty: easy Section: 1.1

2. Compute the indicated value of the given function.

$$f(x) = 5x^2 - 3; f(-1)$$

Ans: 2

Difficulty: easy Section: 1.1

3. Compute the indicated values of the given function.

$$f(x) = x - 3 + |x - 5|; f(-4), f(-3), f(-2).$$

A) 8, 8, 8 B) -2, -2, -2 C) -6, -4, -2 D) 2, 2, 2

Ans: D Difficulty: easy Section: 1.1

4. Compute the indicated value of the given function.

$$f(x) = |x - 3| + x - 5; f(2)$$

A) -4 B) 2 C) -2 D) 1

Ans: C Difficulty: moderate Section: 1.1

5. Compute the indicated value of the given function.

$$f(x) = |x + 2| + 3|x - 1|; f(-3)$$

A) 13 B) -133 C) 9 D) 23

Ans: A Difficulty: moderate Section: 1.1

6. Compute the indicated value of the given function.

$$f(t) = \begin{cases} -3t + 5 & \text{if } t < -1 \\ t^2 + 6 & \text{if } t \geq -1 \end{cases}; f(-3)$$

A) 14 B) -4 C) 15 D) -3

Ans: A Difficulty: easy Section: 1.1

7. Compute the indicated value of the given function.

$$f(x) = \begin{cases} x^2 - 1 & \text{if } x < 1 \\ 3 & \text{if } x = 1; f(2) \\ 2 - 5x & \text{if } x > 1 \end{cases}$$

Ans: -8

Difficulty: moderate Section: 1.1



14. Determine the domain of the given function.

$$f(t) = \frac{\sqrt{t^2 - 1}}{t - 3}$$

Ans: All real numbers  $t$  for which  $t \geq 1$  or  $t \leq -1$  except  $t = 3$

Difficulty: hard Section: 1.1

15. Determine the domain of the given function.

$$f(t) = \frac{\sqrt{t^2 - 4}}{t - 6}$$

Ans: All real numbers  $t$  for which  $t \geq 2$  or  $t \leq -2$  except  $t = 6$ .

Difficulty: hard Section: 1.1

16. Find the composite function  $f(g(x))$ .

$$f(u) = u^3 + 2, g(x) = x + 3$$

A)  $f(g(x)) = x^3 + 5$

C)  $f(g(x)) = x^3 + 9x^2 + 27x + 27$

B)  $f(g(x)) = x^3 + 6$

D)  $f(g(x)) = x^3 + x + 5$

Ans: C Difficulty: easy Section: 1.1

17. Find the composite function  $f(g(x))$ .

$$f(u) = \frac{1}{u} - u, g(x) = 2x - 3$$

Ans:  $f(g(x)) = \frac{-4x^2 + 12x - 8}{2x - 3}$

Difficulty: easy Section: 1.1

18. Find the composite function  $f(g(x))$ .

$$f(u) = \frac{1}{u}, g(x) = x + 3$$

A)  $f(g(x)) = \frac{1}{x} + 3$

C)  $f(g(x)) = 1 + \frac{3}{x}$

B)  $f(g(x)) = x + 3 + \frac{1}{x}$

D)  $f(g(x)) = \frac{1}{x + 3}$

Ans: D Difficulty: easy Section: 1.1

19. Find the difference quotient,  $\frac{f(x+h) - f(x)}{h}$ .

$$f(x) = \frac{5}{x}$$

A)  $\frac{f(x+h) - f(x)}{h} = 1$

C)  $\frac{f(x+h) - f(x)}{h} = -\frac{5}{x(x+h)}$

B)  $\frac{f(x+h) - f(x)}{h} = 5$

D)  $\frac{f(x+h) - f(x)}{h} = \frac{5}{x+h}$

Ans: C      Difficulty: moderate      Section: 1.1

20. Find the indicated composite function.

$$f(x+5) \text{ where } f(x) = \frac{1}{x}$$

A)  $f(x+5) = \frac{1}{x+5}$

C)  $f(x+5) = x+5 + \frac{1}{x}$

B)  $f(x+5) = \frac{1}{x} + 5$

D)  $f(x+5) = 1 + \frac{3}{x}$

Ans: A      Difficulty: easy      Section: 1.1

21. Find the indicated composite function.

$$f(4x-5) \text{ where } f(x) = \frac{1}{x} - x$$

Ans:  $f(4x-5) = \frac{-16x^2 + 40x - 24}{4x-5}$

Difficulty: easy      Section: 1.1

22. Find functions  $h(x)$  and  $g(u)$  such that  $f(x) = g(h(x))$ :

$$f(x) = \sqrt[3]{84 - 7x - 4x^2}$$

Ans:  $h(x) = 84 - 7x - 4x^2$ ;  $g(u) = \sqrt[3]{u}$  is one possible answer.

Difficulty: easy      Section: 1.1

23. Find functions  $h(x)$  and  $g(u)$  such that  $f(x) = g(h(x))$ :

$$f(x) = \frac{5}{\sqrt{x+4}} + 3\sqrt{x+4}$$

Ans:  $h(x) = x+4$ ;  $g(u) = \frac{5}{\sqrt{u}} + 3\sqrt{u}$  is one possible answer.

Difficulty: easy      Section: 1.1

24. An efficiency study of the morning shift at a certain factory indicates that an average worker who arrives on the job at 8:00 A.M. will have assembled  $f(x) = -x^3 + 5x^2 + 16x$  transistor radios  $x$  hours later. How many radios will such a worker assemble between 10:00 and 11:00 A.M.?

A) 20    B) 22    C) 15    D) 18

Ans: B    Difficulty: moderate    Section: 1.1

25. To study the rate at which animals learn, a psychology student performed an experiment in which a rat was sent repeatedly through a laboratory maze. Suppose the time required for the rat to traverse the maze on the  $n$ th trial was approximately  $T(n) = 5 + \frac{2}{n} - \frac{4}{n^2}$  minutes. How many minutes does it take the rat to traverse the maze on the 2nd trial?

Ans:  $T(2) = 5$  min

Difficulty: hard    Section: 1.1

26. To study the rate at which animals learn, a psychology student performed an experiment in which a rat was sent repeatedly through a laboratory maze. Suppose the time required for the rat to traverse the maze on the  $n^{\text{th}}$  trial was approximately  $T(n) = 8 + \frac{4}{n} - \frac{8}{n^2}$  minutes. How long does it take the rat to traverse the maze in the second trial?

Ans:  $T(2) = 8$  minutes

Difficulty: hard    Section: 1.1

27. A ball is thrown upward in such a way that  $t$  seconds later, it is  $H(t) = -16t^2 + 64t + 80$  feet above the ground. How many seconds later does the ball hit the ground?

Ans:  $H(t) = 0$  at  $t = 5$  seconds

Difficulty: hard    Section: 1.1

28. A ball is thrown upward in such a way that  $t$  seconds later it is  $H(t) = -11t^2 + 44t + 55$  feet above the ground. When does the ball hit the ground?

Ans:  $H(t) = 0$  at  $t = 5$  seconds.

Difficulty: hard    Section: 1.1

29. At a certain factory, the total cost of manufacturing  $q$  units during the daily production run is  $C(q) = q^2 + 2q + 297$  dollars. On a typical workday,  $q(t) = 17t$  units are manufactured during the first  $t$  hours of a production run. How many dollars are spent during the first 3 hours of production?

Ans: \$3,000

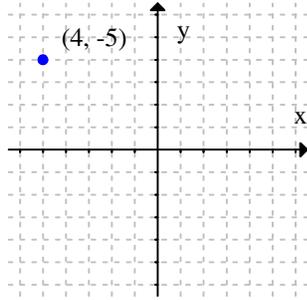
Difficulty: hard    Section: 1.1

30. At a certain factory, the total cost of manufacturing units during the daily production run is  $C(q) = q^2 + 2q + 254$  dollars. On a typical day,  $q(t) = 16t$  units are manufactured during the first hours of a production run. How much is spent during the first 3 hours of production?

Ans: \$2,654

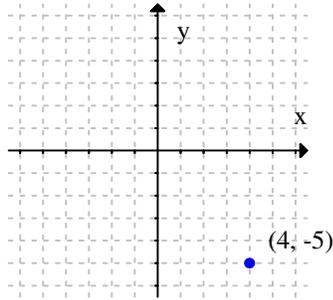
Difficulty: hard      Section: 1.1

31. Plot the given point in a rectangular coordinate system.  
 $(4, -5)$



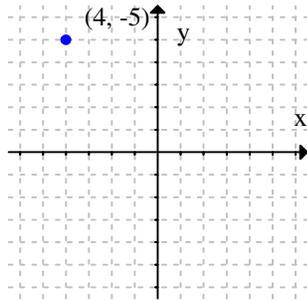
A)

*(Each gridline represents one unit.)*



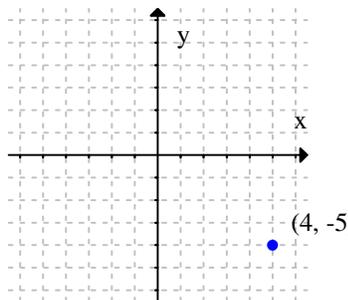
B)

*(Each gridline represents one unit.)*



C)

*(Each gridline represents one unit.)*



D)

(Each gridline represents one unit.)

Ans: B      Difficulty: easy      Section: 1.2

32. Find the distance between the given points.

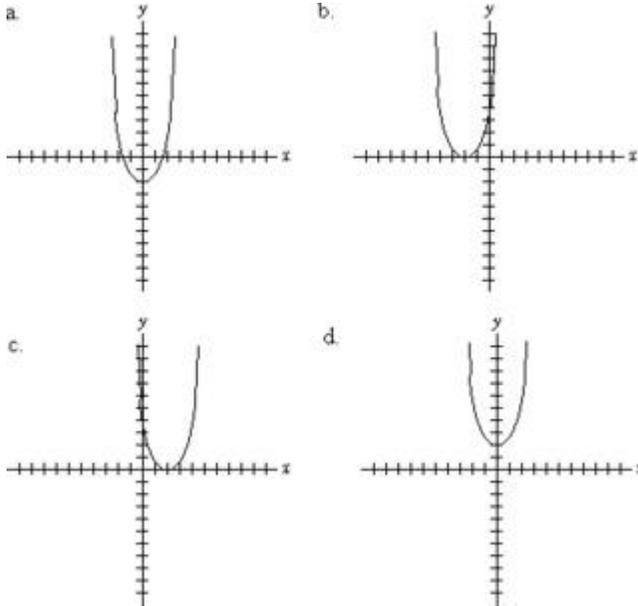
$(-2, 1)$  and  $(7, -5)$

A)  $D = \sqrt{15}$       B)  $D = 15$       C)  $D = 117$       D)  $D = 3\sqrt{13}$

Ans: D      Difficulty: easy      Section: 1.2

33. Sketch the graph of the given function.

$$f(x) = x^2 + 2$$



(Tick marks are spaced one unit apart.)

A) Graph a      B) Graph b      C) Graph c      D) Graph d

Ans: D      Difficulty: moderate      Section: 1.2

34. Find the points of intersection (if any) of the given pair of curves.

$$y = 3x - 1 \text{ and } y = 3 - 5x$$

Ans:  $\left(\frac{1}{2}, \frac{1}{2}\right)$

Difficulty: easy      Section: 1.2

35. Find the points of intersection (if any) of the given pair of curves.

$$y = x + 2 \text{ and } y = 2x + 4$$

A)  $(-2, 0)$       B)  $(1, -4)$       C)  $(0, 6)$       D)  $(0, 2)$

Ans: A      Difficulty: moderate      Section: 1.2

36. Find the points of intersection (if any) of the given pair of curves.

$$y = 7x - 4 \text{ and } y = 3x - 5$$

Ans:  $\left(-\frac{1}{4}, -\frac{23}{4}\right)$

Difficulty: easy      Section: 1.2

37. Find the points of intersection (if any) of the given pair of curves.

$$y = x + 3 \text{ and } y = 2x + 4$$

- A) (1, -4)    B) (-1, 2)    C) (0, 3) and (1, 4)    D) (1, 6)

Ans: B      Difficulty: moderate      Section: 1.2

38. Find the points of intersection (if any) of the given pair of curves.

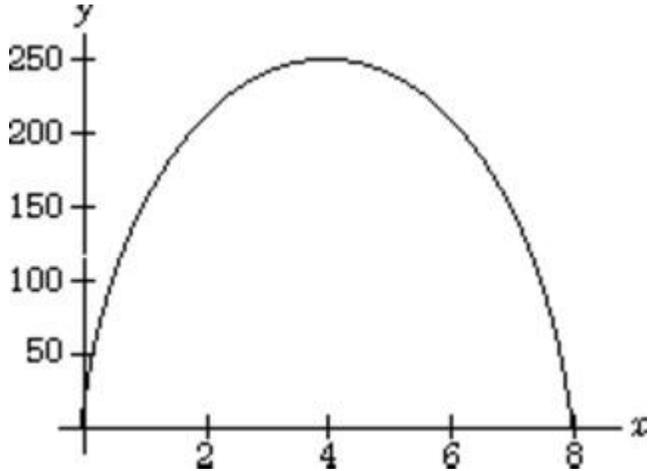
$$y = x^2 \text{ and } y = 3x - 2.$$

- A) (0,0)    B) There are no points of intersection.    C) (2, 4)    D) (1, 1), (2, 4)

Ans: D      Difficulty: moderate      Section: 1.2

39. If an object is thrown vertically upward with an initial speed of 128 ft/sec, its height (in feet)  $t$  seconds later is given by  $H(t) = -16t^2 + 128t$ . Graph the function  $H(t)$  and use the graph to determine when the object will hit the ground.

Ans: 8 seconds



Difficulty: hard      Section: 1.2

40. A ball is thrown upward in such a way that  $t$  seconds later, it is  $s = -16t^2 + 96t + 144$  feet above the ground. Sketch the graph of  $s(t)$  and determine the maximum height in feet attained by the ball.

Ans: 288 ft

Difficulty: hard      Section: 1.2

41. Find the slope (if possible) of the line that passes through the given pair of points.  
 (-1, 5) and (7, 2)

Ans:  $-\frac{3}{8}$

Difficulty: easy Section: 1.3

42. Find the slope (if possible) of the line that passes through the given pair of points.  
 (5, 0) and (3, 4)

A) -2    B) 2    C)  $-\frac{1}{2}$     D)  $\frac{1}{2}$

Ans: A    Difficulty: easy    Section: 1.3

43. Find the slope (if possible) of the line that passes through the given pair of points.  
 (11, 0) and (14, 11)

A)  $\frac{11}{3}$     B)  $\frac{3}{11}$     C)  $-\frac{3}{11}$     D)  $-\frac{11}{3}$

Ans: A    Difficulty: easy    Section: 1.3

44. Find the slope (if possible) of the line that passes through the given pair of points.  
 (19, 10) and (5, 8).

A) 7    B)  $\frac{1}{7}$     C) 0    D) The slope is undefined.

Ans: B    Difficulty: easy    Section: 1.3

45. Find the slope (if possible) of the line that passes through the given pair of points.  
 (6, 7) and (9, -1).

Ans:  $-\frac{8}{3}$

Difficulty: easy    Section: 1.3

46. Find the slope of the line passing through (4, 3) and (0, 4). Round your answer to two decimal places, if necessary.

A) -0.25    B) -4.00    C) 4.00    D) 0.25

Ans: A    Difficulty: easy    Section: 1.3

47. Find the slope and y-intercept of the line whose equation is given.

$$5y = 8x$$

A) slope 8, y-intercept 0                      C) slope  $\frac{8}{5}$ , y-intercept 0  
 B) slope 8, y-intercept 5                      D) slope  $-\frac{8}{5}$ , y-intercept 0

Ans: C    Difficulty: moderate    Section: 1.3

48. Find the slope and y-intercept (if they exist) of the line  $2y = 9x$ .

- A) Slope is  $\frac{9}{2}$  and y-intercept is 0.      C) Slope is 9 and y-intercept is 0.  
 B) Slope is 9 and y-intercept is 2.      D) Slope is  $\frac{2}{9}$  and y-intercept is 0.

Ans: A      Difficulty: easy      Section: 1.3

49. Find the slope and y-intercept of the line whose equation is given.

$$y = 2x - 5.$$

- A) slope 2, y-intercept  $-5$       C) slope  $\frac{1}{2}$ , y-intercept  $-5$   
 B) slope 2, y-intercept 5      D) slope  $\frac{1}{2}$ , y-intercept 5

Ans: A      Difficulty: easy      Section: 1.3

50. Find the slope of the line whose equation is given.

$$3x + 5y = -7$$

Ans:  $-\frac{3}{5}$

Difficulty: moderate      Section: 1.3

51. Find the slope of the line whose equation is given.

$$3x - 5y = 9.$$

Ans:  $\frac{3}{5}$

Difficulty: moderate      Section: 1.3

52. What is the slope of the line  $7x + 8y = -3$ ? Round your answer to two decimal places, if necessary.

- A)  $-1.14$     B)  $1.14$     C)  $0.88$     D)  $-0.88$

Ans: D      Difficulty: easy      Section: 1.3

53. Find the slope of the line with the following equation  $9x + 4y = -8$ .

Ans: Slope:  $-\frac{9}{4}$

Difficulty: moderate      Section: 1.3

54. Find the slope and y-intercept of the line  $3y - 7x = 1$ .

Ans: Slope:  $\frac{7}{3}$ ; y-intercept:  $\frac{1}{3}$

Difficulty: moderate      Section: 1.3

55. Find the slope and y-intercept of the line whose equation is given.

$$\frac{x}{3} + \frac{y}{5} = 1$$

Ans: Slope:  $-\frac{5}{3}$ ; y-intercept: 5

Difficulty: hard Section: 1.3

56. Find the slope and y-intercept of the line whose equation is given.

$$\frac{x}{2} + \frac{y}{3} = 1$$

A) Slope:  $-\frac{3}{2}$ ; y-intercept: 3

C) Slope:  $\frac{1}{2}$ ; y-intercept: 1

B) Slope:  $\frac{3}{2}$ ; y-intercept: 1

D) Slope:  $\frac{3}{2}$ ; y-intercept:  $\frac{1}{2}$

Ans: A Difficulty: moderate Section: 1.3

57. Write an equation for the line through (3, 0) with slope 2.

A)  $y = 2x - 6$  B)  $y = 2x - 3$  C)  $y = 2x + 6$  D)  $y = 2x + 3$

Ans: A Difficulty: moderate Section: 1.3

58. Write an equation for the line with the given properties.

Through (3, -1) with slope 2

Ans:  $y = 2x - 7$

Difficulty: moderate Section: 1.3

59. Write an equation for the line through (5, 4) and parallel to the x-axis.

A)  $x = 5$  B)  $x = -5$  C)  $y = 4$  D)  $y = -4$

Ans: C Difficulty: easy Section: 1.3

60. Find an equation of the line parallel to the line y-axis and through the point (3, 9).

Ans:  $x = 3$ .

Difficulty: moderate Section: 1.3

61. What is the equation of the line through the points (7, -3) and (5, 19)? Round numbers to two decimal places, if necessary.

A)  $y = -0.09x + 74$  C)  $y = -11x + 0.01$

B)  $y = -0.09x + 0.01$  D)  $y = -11x + 74$

Ans: D Difficulty: easy Section: 1.3

62. Between August 29 and September 4, 2005, the price of gasoline increased steadily due to the impact of hurricane Katrina. The average price per gallon in Cincinnati on August 29 was \$2.60, and on September 4 it was \$3.10. Write a linear function  $C(x)$  that describes the cost per gallon of gas in Cincinnati in terms of days after August 29. Round the slope to three decimal places, if necessary. Use your function to find how much gas would have cost on October 1 if the price had continued to increase at that rate.  
 Ans:  $C(x) = 0.083x + 2.60$ ; \$5.34  
 Difficulty: moderate Section: 1.3
63. The cost of renting a backhoe at one distributor is \$335, plus \$35 per day. Write a linear function  $C(x)$  that describes the cost of renting the backhoe for  $x$  days, then use your function to find how much it would cost to rent it for 7 days.  
 A)  $C(x) = 335x + 35$ ; \$2,380      C)  $C(x) = 335 + 35x$ ; \$580  
 B)  $C(x) = 7(335 + 35x)$ ; \$4,060      D)  $C(x) = 35x + 328$ ; \$573  
 Ans: C Difficulty: easy Section: 1.3
64. Each unit of a certain commodity costs  $p = 11x + 12$  cents when  $x$  units of the commodity are produced. If all units are sold at this price, express the revenue derived from the sales as a function of  $x$ .  
 A)  $x(11x + 12)$  cents      C)  $11x^2 + 12$  cents  
 B)  $10x + 12$  cents      D)  $12x + 12$  cents  
 Ans: A Difficulty: hard Section: 1.4
65. A manufacturer's total cost consists of a fixed overhead of \$250 plus production costs of \$70 per unit. Express the total cost in dollars as a function of the number of units produced.  
 Ans:  $C(x) = 70x + 250$   
 Difficulty: hard Section: 1.4
66. A manufacturer's total cost consists of a fixed overhead of \$350 plus production costs of \$60 per unit. Express the total cost in dollars as a function of the number of units produced.  
 Ans:  $C(x) = 60x + 350$ .  
 Difficulty: hard Section: 1.4
67. A farmer is planning to plant a rectangular garden with an area of 4,000 square yards. The garden is to be fenced on all four sides. Express the number of yards of fencing required as a function of  $x$ , the long side of the fence.  
 Ans:  $s = 2x + 2\left(\frac{4,000}{x}\right)$   
 Difficulty: hard Section: 1.4

68. A farmer is planning to plant a rectangular garden with an area of 400 square yards. The garden is to be fenced on all four sides. Express the number of yards of fencing required as a function of  $x$ , the long side of the fence.

$$\text{Ans: } 2x + \frac{800}{x}$$

Difficulty: hard      Section: 1.4

69. A rectangle is constructed inside a circle of radius  $r$  with the corners of the rectangle lying on the circle. Express the area  $A$  of the rectangle as a function of the radius  $r$  if the width of one side of the rectangle is 2.

$$\text{Ans: } A = 4\sqrt{r^2 - 1}$$

Difficulty: moderate      Section: 1.4

70. A closed cylindrical can has a surface area of  $360\pi$  square inches. Express the volume of the can as a function of its radius,  $r$ .

$$\text{A) } V(r) = \pi r(180 - r^2) \text{ cubic inches} \quad \text{C) } V(r) = 360\pi r^2 \text{ cubic inches}$$

$$\text{B) } V(r) = 180\pi r \text{ cubic inches} \quad \text{D) } V(r) = \pi(180 - r^3) \text{ cubic inches}$$

Ans: A      Difficulty: hard      Section: 1.4

71. A cylindrical can is to have a volume of  $36\pi$  cubic inches. The cost of the material used for the top and bottom of the can is 4 cents per square inch, and the cost of the material used for the curved side is 3 cents per square inch. Express the cost in cents of constructing the can as a function of its radius.

$$\text{Ans: } C = 8\pi r^2 + \frac{216\pi}{r}$$

Difficulty: hard      Section: 1.4

72. A cylindrical can is to have a volume of  $45\pi$  cubic inches. The cost of the material used for the top and bottom of the can is 4 cents per square inch, and the cost of the material used for the curved side is 5 cents per square inch. Express the cost of constructing the can as a function of its radius.

$$\text{Ans: } 8\pi r^2 + 450\frac{\pi}{r} \text{ cents}$$

Difficulty: hard      Section: 1.4

73. A closed box with a square base is to have a volume of 20 cubic meters. The material for the top and bottom of the box costs \$3 per square meter, and the material for the sides costs \$1 per square meter. Express the construction cost of the box as a function of the length of its base,  $x$ .

A)  $C(x) = x^2 + 80x + 2$  dollars      C)  $C(x) = 2x^2 + \frac{20}{x}$  dollars  
 B)  $C(x) = 2x^2 + \frac{2}{x} + 6$  dollars      D)  $C(x) = 6x^2 + \frac{80}{x}$  dollars

Ans: D      Difficulty: hard      Section: 1.4

74. The supply and demand functions,  $S(x)$  and  $D(x)$ , respectively, for a certain commodity are given in terms of the level of production  $x$ .  $S(x) = 2x + 30$ ,  $D(x) = 360 - x$ . Find the value of  $x_e$  for which equilibrium occurs.

Ans: 110

Difficulty: easy      Section: 1.4

75. Two car rental agencies are competing. One agency rents cars for 35 dollars per day and 35 cents a mile; the other agency rents cars for 30 dollars per day and 50 cents a mile. For a 9 day trip, how many miles must you travel to have the total cost be the same with each agency? Round to the nearest whole mile, if necessary.

A) 300 miles    B) 33 miles    C) 14 miles    D) 10 miles

Ans: A      Difficulty: hard      Section: 1.4

76. Two jets bound for San Diego leave Boston 20 minutes apart. The first travels at 450 miles per hour, while the second goes 500 miles per hour. How many hours after the second plane departs will the second plane pass the first?

Ans: 3 hours after the second plane leaves

Difficulty: hard      Section: 1.4

77. Two jets bound for San Diego leave Boston 20 minutes apart. The first plane travels at 300 miles per hour, while the second plane goes 320 miles per hour. At what time will the second plane pass the first?

Ans: 5 hours after the second plane departs.

Difficulty: hard      Section: 1.4

78. An appliance manufacturer can sell refrigerators for \$600 apiece. The manufacturer's total cost consists of a fixed overhead of \$12,000 plus production cost of \$400 per refrigerator. How many refrigerators must be sold for the manufacturer to break even?

Ans: 60

Difficulty: hard      Section: 1.4

79. An appliance manufacturer can sell refrigerators for \$600 apiece. The manufacturer's total cost consists of a fixed overhead of \$12,000 plus production cost of \$400 per refrigerator. How many refrigerators must be sold for the manufacturer to break even?

Ans: 60

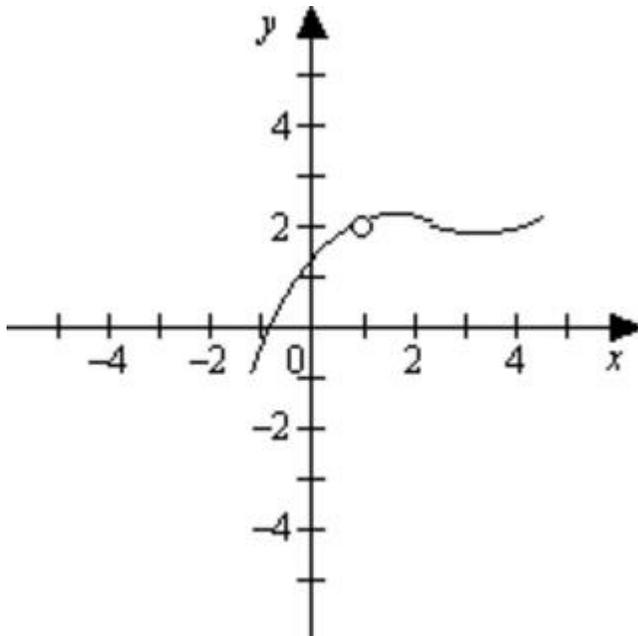
Difficulty: hard Section: 1.4

80. A company makes a certain product for \$4 each and sells it for \$8. If the company has overhead expenses of \$10,000 per year, how many of its products must be made and sold to break even?

A) 10,000 B) 20,000 C) 40,000 D) 2,500

Ans: D Difficulty: hard Section: 1.4

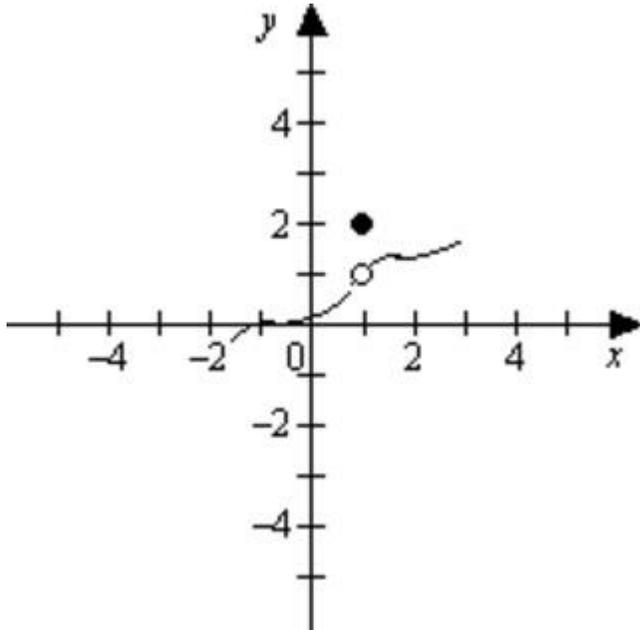
81. If  $f(x)$  is graphed below, find  $\lim_{x \rightarrow 1} f(x)$  if it exists.



Ans: 2

Difficulty: moderate Section: 1.5

82. If  $f(x)$  is graphed below, find  $\lim_{x \rightarrow 1} f(x)$  if it exists.



Ans: 1

Difficulty: moderate Section: 1.5

83. Find the indicated limit if it exists.

$$\lim_{x \rightarrow 1} (2x^2 - 3x + 1)$$

Ans: 0

Difficulty: easy Section: 1.5

84. Find the indicated limit if it exists.

$$\lim_{x \rightarrow 1} (3x^2 - 8x + 1)$$

Ans: -4

Difficulty: easy Section: 1.5

85. Find the indicated limit if it exists.

$$\lim_{x \rightarrow 3} (x + 4)$$

A) 7 B) 3 C) Does not exist D) -1

Ans: A Difficulty: easy Section: 1.5

86. Find the indicated limit if it exists.

$$\lim_{x \rightarrow 1} \frac{2x-1}{x+3}$$

Ans:  $\frac{1}{4}$

Difficulty: easy Section: 1.5

87. Find the indicated limit if it exists.

$$\lim_{x \rightarrow 2} \frac{x-2}{x^2-4}$$

Ans:  $\frac{1}{4}$

Difficulty: moderate      Section: 1.5

88. Find the indicated limit if it exists.

$$\lim_{x \rightarrow 1} \frac{3x^2 - 5x + 2}{2x + 1}$$

Ans: 0

Difficulty: easy      Section: 1.5

89. Find the indicated limit if it exists.

$$\lim_{x \rightarrow 1} \frac{2x-1}{x+4}$$

Ans:  $\frac{1}{5}$

Difficulty: easy      Section: 1.5

90. Find the indicated limit if it exists.

$$\lim_{x \rightarrow 2} \frac{x-2}{x^2-4}$$

Ans:  $\frac{1}{4}$

Difficulty: moderate      Section: 1.5

91. Find the indicated limit if it exists.

$$\lim_{x \rightarrow 1} \frac{x^2 + 3x + 2}{x^2 - 1}$$

A)  $\frac{3}{2}$     B) 3    C) 6    D) Does not exist

Ans: D      Difficulty: moderate      Section: 1.5

92. Find the indicated limit if it exists.

$$\lim_{x \rightarrow 4} \frac{\sqrt{x} - 2}{x - 4}$$

A) Does not exist    B) 4    C)  $-\frac{1}{4}$     D)  $\frac{1}{4}$

Ans: D      Difficulty: hard      Section: 1.5

93. Find  $\lim_{x \rightarrow +\infty} f(x)$  and  $\lim_{x \rightarrow -\infty} f(x)$ . If the limiting value is infinite indicate whether it is  $+\infty$  or  $-\infty$ .

$$f(x) = (8 - 3x)(x + 4)$$

- A)  $-\infty, 0$     B)  $+\infty, 0$     C)  $-\infty, -\infty$     D)  $+\infty, +\infty$

Ans: C    Difficulty: moderate    Section: 1.5

94. Find  $\lim_{x \rightarrow +\infty} f(x)$  and  $\lim_{x \rightarrow -\infty} f(x)$ . If the limiting value is infinite indicate whether it is  $+\infty$  or  $-\infty$ .

$$f(x) = \frac{1 - 4x^3}{5x^3 - 9x - 3}$$

- A)  $-\frac{4}{5}, \frac{4}{5}$     B)  $-\frac{4}{5}, -\frac{4}{5}$     C)  $+\infty, -\infty$     D)  $-\infty, +\infty$

Ans: B    Difficulty: moderate    Section: 1.5

95. Complete the table by evaluating  $f(x)$  at the specified values of  $x$ . Then use the table to estimate the indicated limit, or show that it does not exist.

$$f(x) = 2x^2 - 9x; \quad \lim_{x \rightarrow 5} f(x)$$

$x$	4.9	4.99	4.999	5	5.001	5.01	5.1
$f(x)$				×			

Ans:

$x$	4.9	4.99	4.999	5	5.001	5.01	5.1
$f(x)$	3.92	4.8902	4.989002	×	5.011002	5.1102	6.12

$$\lim_{x \rightarrow 5} f(x) = 5$$

Difficulty: easy    Section: 1.5

96. Complete the table by evaluating  $f(x)$  at the specified values of  $x$ . Then use the table to estimate the indicated limit, or show that it does not exist.

$$f(x) = \frac{3x^2 - 48}{x + 4}; \quad \lim_{x \rightarrow -4} f(x)$$

$x$	-4.1	-4.01	-4.001	-4	-3.999	-3.99	-3.9
$f(x)$				×			

Ans:

$x$	-4.1	-4.01	-4.001	-4	-3.999	-3.99	-3.9
$f(x)$	-24.3	-24.03	-24.003	×	-23.997	-23.97	-23.7

$$\lim_{x \rightarrow -4} f(x) = -24$$

Difficulty: easy    Section: 1.5

97. Complete the table by evaluating  $f(x)$  at the specified values of  $x$ . Then use the table to estimate the indicated limit, or show that it does not exist.

$$f(x) = \frac{3x+5}{x-4}; \quad \lim_{x \rightarrow 4} f(x)$$

$x$	3.9	3.99	3.999	4	4.001	4.01	4.1
$f(x)$				X			

Ans: 

$x$	3.9	3.99	3.999	4	4.001	4.01	4.1
$f(x)$	-167	-1,697	-16,997	X	17,003	1,703	173

$\lim_{x \rightarrow 4} f(x)$  does not exist

Difficulty: easy      Section: 1.5

98. An efficiency consultant determines that when new workers are hired to wait tables at an upscale restaurant, the average number of tables they can wait on in a 6 hour shift is given by

$$N(x) = \frac{\sqrt{5.3x^2 + 50x + 14}}{0.1x + 0.8}$$

where  $x$  is the number of shifts they've worked since being hired. What happens to an average waiter's productivity in the long run (as  $x \rightarrow \infty$ )?

- A) It approaches 14 tables per shift.      C) It approaches 53 tables per shift.  
 B) It approaches 23 tables per shift.      D) It increases without bound.

Ans: B      Difficulty: moderate      Section: 1.5

99. As a rumor spreads across a college campus, the number of people that have heard it can be modeled by the equation

$$N(t) = \frac{7,600t^2 + 3,800t}{(t+3)^2}$$

where  $t$  is days since the rumor started spreading. What happens to the number of people that have heard the rumor in the long run (as  $t \rightarrow \infty$ )?

Ans: It approaches 7,600.

Difficulty: easy      Section: 1.5

100. Find the indicated one-sided limit. If the limiting value is infinite, indicate whether it is  $+\infty$  or  $-\infty$ .

$$\lim_{x \rightarrow 4^-} \frac{\sqrt{x} - 2}{x - 4}$$

- A) 2    B) -2    C)  $\frac{1}{4}$     D)  $-\frac{1}{4}$

Ans: C      Difficulty: hard      Section: 1.6

101. Find the indicated one-sided limit. If the limiting value is infinite, indicate whether it is  $+\infty$  or  $-\infty$ .

$$\lim_{x \rightarrow 36^-} \frac{\sqrt{x} - 6}{x - 36}$$

Ans:  $\frac{1}{12}$

Difficulty: hard      Section: 1.6

102. Find the indicated one-sided limit. If the limiting value is infinite, indicate whether it is  $+\infty$  or  $-\infty$ .

$$\lim_{x \rightarrow 9^-} \frac{\sqrt{x} - 3}{x - 9}$$

Ans:  $\frac{1}{6}$

Difficulty: hard      Section: 1.6

103. Find the indicated one-sided limit. If the limiting value is infinite, indicate whether it is  $+\infty$  or  $-\infty$ .

$$\lim_{x \rightarrow 1^+} \frac{\sqrt{x-1}}{x-1}$$

Ans:  $+\infty$

Difficulty: hard      Section: 1.6

104. Find the indicated one-sided limit. If the limiting value is infinite, indicate whether it is  $+\infty$  or  $-\infty$ .

$$\lim_{x \rightarrow 6^+} \frac{\sqrt{x-6}}{x-6}$$

Ans:  $+\infty$

Difficulty: hard      Section: 1.6

105. Find the indicated one-sided limit. If the limiting value is infinite, indicate whether it is  $+\infty$  or  $-\infty$ .

$$\lim_{x \rightarrow 2^-} f(x) \text{ where } f(x) = \begin{cases} x^2 & \text{if } x \leq 2 \\ x+1 & \text{if } x > 2 \end{cases}$$

Ans: 4

Difficulty: hard      Section: 1.6

106. Find the indicated one-sided limit. If the limiting value is infinite, indicate whether it is  $+\infty$  or  $-\infty$ .

$$\lim_{x \rightarrow 2^+} f(x) \text{ where } f(x) = \begin{cases} x^2 & \text{if } x \leq 2 \\ x+1 & \text{if } x > 2 \end{cases}$$

Ans: 3

Difficulty: hard Section: 1.6

107. Find the indicated one-sided limit. If the limiting value is infinite, indicate whether it is  $+\infty$  or  $-\infty$ .

$$\lim_{x \rightarrow 2^-} f(x) \text{ where } f(x) = \begin{cases} x+5 & \text{if } x < 2 \\ x^2 & \text{if } x \geq 2 \end{cases}$$

A) 7 B) 0 C) 4 D) There is none

Ans: A Difficulty: hard Section: 1.6

108. True or False:  $\lim_{x \rightarrow 3^-} f(x) = 3$  where  $f(x) = \begin{cases} x & \text{if } x < 3 \\ x+1 & \text{if } x \geq 3 \end{cases}$

A) True B) False

Ans: A Difficulty: hard Section: 1.6

109. Find the indicated one-sided limit. If the limiting value is infinite, indicate whether it is  $+\infty$  or  $-\infty$ .

$$\lim_{x \rightarrow 4^-} f(x) \text{ where } f(x) = \begin{cases} x^2 & \text{if } x \leq 4 \\ x+8 & \text{if } x > 4 \end{cases}$$

Ans: 16

Difficulty: hard Section: 1.6

110. List all values of  $x$  for which  $f(x)$  is not continuous.

$$f(x) = \frac{10x-15}{x-5}$$

Ans: 5

Difficulty: moderate Section: 1.6

111. List all values of  $x$  for which  $f(x)$  is not continuous.

$$f(x) = \frac{5x-10}{x-2}$$

Ans: 2

Difficulty: moderate Section: 1.6

112. List all values of  $x$  for which  $f(x)$  is not continuous.

$$f(x) = \frac{5x+1}{x^2}$$

Ans: 0

Difficulty: moderate      Section: 1.6

113. List all values of  $x$  for which  $f(x)$  is not continuous.

$$f(x) = \frac{2x+1}{x^2+x}$$

A)  $-1$     B)  $0$  and  $-1$     C)  $-\frac{1}{2}$     D) None

Ans: B      Difficulty: moderate      Section: 1.6

114. List all values of  $x$  for which  $f(x)$  is not continuous.

$$f(x) = \frac{6x+6}{x^2}$$

Ans: 0

Difficulty: moderate      Section: 1.6

115. Find all values of  $x$  for which the given function is not continuous.

$$f(x) = \frac{x^2+3x+2}{x^2+4x+3}$$

Ans:  $-1$  and  $-3$

Difficulty: hard      Section: 1.6

116. Decide if the given function is continuous at the specified value of  $x$ .

$$f(x) = \begin{cases} x+5 & \text{if } x < 1 \\ 3x+3 & \text{if } x \geq 1 \end{cases}; \quad x=1$$

A) No, the function is not continuous at  $x = 1$ .

B) Yes, the function is continuous at  $x = 1$ .

Ans: B      Difficulty: easy      Section: 1.6

117. List all the values of  $x$  for which the given function is not continuous.

$$f(x) = \begin{cases} x^2 & \text{if } x \leq 2 \\ 4 & \text{if } x > 2 \end{cases}$$

A)  $x = 0$     B)  $x = 2$     C)  $x = \pm 2$     D) The function is continuous for all values of  $x$ .

Ans: D      Difficulty: easy      Section: 1.6

118. Find all the values of  $x$  for which the given function is not continuous.

$$f(x) = \begin{cases} x^2 + 4 & \text{if } x \leq 5 \\ 4 & \text{if } x > 5 \end{cases}$$

Ans: 5

Difficulty: moderate      Section: 1.6

119. Find all the values of  $x$  for which the given function is not continuous.

$$f(x) = \begin{cases} x^2 + 5 & \text{if } x \leq 5 \\ 2 & \text{if } x > 5 \end{cases}$$

Ans: 5

Difficulty: moderate      Section: 1.6